



2008 Mathematics

Intermediate 1 Units 1, 2 & 3 Paper 2

Finalised Marking Instructions

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Mathematics Intermediate 1: Paper 2, Units 1, 2 and 3

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
1 (a)	Ans: diagram <ul style="list-style-type: none"> •¹ communicate: plot point •² communicate: plot points 	<ul style="list-style-type: none"> •¹ plot A or B or C •² plot other two points <p style="text-align: right;">2 marks</p>
(b)	Ans: D(3,2) plotted <ul style="list-style-type: none"> •¹ strategy: plot 4th vertex of square 	<ul style="list-style-type: none"> •¹ plot(3,2) <p style="text-align: right;">1 mark</p>
<p>NOTES:</p> <ol style="list-style-type: none"> 1. Accept (3,2) if D not plotted 2. If D(3,2) is plotted but wrong coordinates are stated then award 1/1 3. Where (y,x) is consistently plotted <ul style="list-style-type: none"> - award 1/2 for (a) - award 1/1 for (b) for plotting 4th vertex of square 		

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •																		
2 (a)	Ans: £841 • ¹ interpret: find basic premium	• ¹ 841 <p style="text-align: right;">1 mark</p>																		
NOTES: 1. Working subsequent to “correct” answer e.g. $841 \div 12 = 70.08$ award 0/1																				
2 (b)	Ans: £277.53 • ¹ interpret/strategy/process: find discount • ² strategy/process: find net premium	• ¹ $\frac{67}{100} \times 841 = 563.47$ • ² 277.53 <p style="text-align: right;">2 marks</p>																		
NOTES: 1. Some common answers <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 30%;"></th> <th style="width: 35%; text-align: center;"><u>with working</u></th> <th style="width: 35%; text-align: center;"><u>without working</u></th> </tr> </thead> <tbody> <tr> <td>(a) 277.53</td> <td style="text-align: center;">2/2</td> <td style="text-align: center;">2/2</td> </tr> <tr> <td>(b) 563.47</td> <td style="text-align: center;">1/2</td> <td style="text-align: center;">1/2</td> </tr> <tr> <td>(c) 277.50 (841 – 563.50)</td> <td style="text-align: center;">1/2</td> <td style="text-align: center;">1/2</td> </tr> <tr> <td>(d) 278 (841 – 563)</td> <td style="text-align: center;">1/2</td> <td style="text-align: center;">1/2</td> </tr> <tr> <td>(e) 563.50, 563</td> <td style="text-align: center;">see note 2</td> <td style="text-align: center;">0/2</td> </tr> </tbody> </table> 2. (i) $\frac{67}{100} \times 841 = 563.47 = 563.50$ or 563 award 1 st mark (ii) $\frac{67}{100} \times 841 = 563.50$ or 563 do not award 1 st mark				<u>with working</u>	<u>without working</u>	(a) 277.53	2/2	2/2	(b) 563.47	1/2	1/2	(c) 277.50 (841 – 563.50)	1/2	1/2	(d) 278 (841 – 563)	1/2	1/2	(e) 563.50, 563	see note 2	0/2
	<u>with working</u>	<u>without working</u>																		
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(d) 278 (841 – 563)	1/2	1/2																		
(e) 563.50, 563	see note 2	0/2																		

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
3 (a)	Ans: $20u + 7$ • ¹ process: multiply out brackets • ² process: collect like terms	• ¹ $20u - 8 + 15$ or $20u - 8$ • ² $20u + 7$ 2 marks
NOTES: 1. Do not award 1 st mark for $20u - 8 + 60$ 2. $20u - 23$, $20u + 13$ (no working necessary) award 1/2 3. $20 - 8 + 15 = 27$ award 0/2 4. Where a candidate creates and then tries to solve an equation the 2 nd mark cannot be awarded		
3 (b)	Ans: $3(3c + 8)$ • ¹ process: identify common factor • ² process: factorise	• ¹ 3 or $3c + 8$ • ² $3(3c + 8)$ 2 marks
NOTES: 1. $9(c + 2 \cdot 7)$, $9(c + 2 \cdot 66 \dots)$ award 1/2 2. $9(c + 2 \cdot 6)$ award 0/2 [24 ÷ 9 = 2 remainder 6]		

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •												
4 (a)	Ans: 2·5 • ¹ strategy: know to order numbers • ² process: find median	• ¹ 1 1 1 2 2 3 3 4 6 7 • ² 2·5 <p style="text-align: right;">2 marks</p>												
NOTES: 1. Answer <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 33%;"></th> <th style="width: 33%; text-align: center;"><u>with valid working</u></th> <th style="width: 33%; text-align: center;"><u>without valid working</u></th> </tr> </thead> <tbody> <tr> <td>2·5</td> <td style="text-align: center;">2/2</td> <td style="text-align: center;">2/2</td> </tr> <tr> <td>4 (numbers not ordered)</td> <td style="text-align: center;">1/2</td> <td style="text-align: center;">0/2</td> </tr> <tr> <td>3 (mean)</td> <td style="text-align: center;">1/2</td> <td style="text-align: center;">0/2</td> </tr> </tbody> </table> 2. If “correct” median is found from ordered list with one missing (or one extra) number award 1/2 3. Accept ordered list written in part (a) or part (b)				<u>with valid working</u>	<u>without valid working</u>	2·5	2/2	2/2	4 (numbers not ordered)	1/2	0/2	3 (mean)	1/2	0/2
	<u>with valid working</u>	<u>without valid working</u>												
2·5	2/2	2/2												
4 (numbers not ordered)	1/2	0/2												
3 (mean)	1/2	0/2												
4 (b)	Ans: 6 • ¹ strategy/process: find range	• ¹ 6 <p style="text-align: right;">1 mark</p>												
NOTES:														
4 (c)	Ans: Less weeds remain with Noweed. Number of remaining weeds vary more with Noweed. • ¹ interpret/communicate: interpret calculated statistics • ² interpret/communicate: interpret calculated statistics	• ¹ Less weeds remain with Noweed or Noweed is a better weedkiller, etc. • ² Number of remaining weeds vary more with Noweed. <p style="text-align: right;">2 marks</p>												
NOTES: 1. Answer must be consistent with answers to parts (a) and (b) 2. Do not accept eg Weedclear’s median is more Noweed’s range is more														

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
5	<p>Ans: 36 mph</p> <ul style="list-style-type: none"> •¹ strategy/process: calculate distance on motorway •² strategy/process: find distance on other roads •³ strategy: know how to find speed on other roads •⁴ process: calculate speed 	<ul style="list-style-type: none"> •¹ $2 \times 68 = 136$ •² $D = 54$ •³ $S = 54 \div 1\text{h } 30\text{m}$ •⁴ $54 \div 1.5 = 36$ <p style="text-align: right;">4 marks</p>

NOTES:

1. Answers without working

(a) 36	award 4/4	
(b) 136	award 1/4	✓xxx

2. For a **final answer** of 54

(a) 54 [190 – 136]	award 2/4	✓✓xx
(b) 54(·2...) [190 ÷ 3·5]	award 1/4	xxx✓
(c) 54 with no working	award 1/4	xxx✓

3. Examples of answers (working must be shown)

(a) 42, 41(·...)	[54 ÷ 1·3]	3/4 (disregard incorrect rounding)	✓✓✓x
(b) 0·6	[54 ÷ 90]	3/4	✓✓✓x
(c) 0·4...	[54 ÷ 130]	3/4	✓✓✓x
(d) 81	[54 × 1·5]	3/4	✓✓x✓
(e) 4860	[54 × 90]	2/4	✓✓xx
(f) 70(·2)	[54 × 1·3]	2/4	✓✓xx
(g) 7020	[54 × 130]	2/4	✓✓xx
(i) 81(·3...)	[(190–68)÷1·5]	3/4	x✓✓✓
(j) 1·3(5...)	[(190–68)÷90]	2/4	x✓✓x
(k) 94, 93(·...)	[(190–68)÷1·3]	2/4	x✓✓x
(l) 1, 0·9(...)	[(190–68)÷130]	2/4	x✓✓x
(m) 183	[(190–68)×1·5]	2/4	x✓x✓
(n) 10980	[(190–68) ×90]	1/4	x✓xx
(o) 159,158·6	[(190–68) ×1·3]	1/4	x✓xx
(p) 15860	[(190–68) ×130]	1/4	x✓xx
(q) 91, 90(·...)	[(68×2)÷1·5]	3/4	✓x✓✓
(r) 127, 126(·...)	[190÷1·5]	2/4	xx✓✓
(s) 34	[68÷2]	0/4	

4. 4th mark is not available for division by a whole number.

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •								
6	<p>Ans: 77</p> <ul style="list-style-type: none"> •¹ strategy/process: find angle at centre of “beetles” sector •² strategy: know how to find number of beetles •³ process: find number of beetles 	<ul style="list-style-type: none"> •¹ 126 •² $\frac{126}{360} \times 220$ •³ 77 <p style="text-align: right;">3 marks</p>								
	<p>Alternative Strategy</p> <ul style="list-style-type: none"> •¹ strategy: know to calculate 220 – (flies + ants + spiders) •² strategy: know how to find number of flies, ants and spiders •³ process: find number of beetles 	<ul style="list-style-type: none"> •¹ 220 – (flies + ants + spiders) •² flies = 220 ÷ 2, ants = 220 ÷ 10, spiders = ants ÷ 2 or equivalent •³ 77 <p style="text-align: right;">3 marks</p>								
<p>NOTES:</p> <table style="width: 100%; border: none;"> <tr> <td style="width: 60%;">1. Correct answer without working</td> <td style="width: 40%;">award 3/3</td> </tr> <tr> <td>2. 143 [flies + ants + spiders] (no working necessary)</td> <td>award 2/3</td> </tr> <tr> <td>3. 57 [$\frac{126}{220} \times 100$] (no working necessary)</td> <td>award 1/3</td> </tr> <tr> <td>4. $\frac{1}{3}$ of 220 = 73(·3...)</td> <td>award 0/3</td> </tr> </table>			1. Correct answer without working	award 3/3	2. 143 [flies + ants + spiders] (no working necessary)	award 2/3	3. 57 [$\frac{126}{220} \times 100$] (no working necessary)	award 1/3	4. $\frac{1}{3}$ of 220 = 73(·3...)	award 0/3
1. Correct answer without working	award 3/3									
2. 143 [flies + ants + spiders] (no working necessary)	award 2/3									
3. 57 [$\frac{126}{220} \times 100$] (no working necessary)	award 1/3									
4. $\frac{1}{3}$ of 220 = 73(·3...)	award 0/3									

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
7	<p>Ans: 117 cm</p> <ul style="list-style-type: none"> •¹ strategy: correct form of Pythagoras Theorem •² process: calculate sum of two squares •³ process: calculate square root of sum (or difference) of two squares •⁴ strategy/process: add 20 to previously calculated value 	<ul style="list-style-type: none"> •¹ $80^2 + 55^2$ •² 9425 (the only cases where this mark is available for calculating the difference of two squares are shown in notes 2a and 3b) •³ 97(.08...) (correctly rounded or truncated) •⁴ 117 <p style="text-align: right;">4 marks</p>

NOTES:

1. Some common answers (no working necessary)

(a)	117	4/4	
(b)	97	3/4	✓✓✓×

2. Some common answers (working must be shown) where correct horizontal distance of 80 is used

(a)	78(...)	[$\sqrt{(80^2 - 55^2)} + 20$]	3/4	×✓✓✓
(b)	156(...)	[$\sqrt{(80^2 + 110^2)} + 20$]	3/4	×✓✓✓
(c)	95(...)	[$\sqrt{(110^2 - 80^2)} + 20$]	2/4	××✓✓

3. Some common answers (working must be shown) where incorrect horizontal distance of $80+20=100$ is used
 [4th mark is unavailable since 20 has been added inappropriately]

(a)	114(...)	[$\sqrt{(100^2 + 55^2)}$]	3/4	✓✓✓×
(b)	84,83(...)	[$\sqrt{(100^2 - 55^2)}$]	2/4	×✓✓×
(c)	149,148(...)	[$\sqrt{(100^2 + 110^2)}$]	2/4	×✓✓×
(d)	46,45(...)	[$\sqrt{(110^2 - 100^2)}$]	1/4	××✓×

4. Award of first 2 marks if trigonometry is used:

(a)	55 ÷ sin($\tan^{-1}(55/80)$) or 80 ÷ cos($\tan^{-1}(55/80)$)	award marks 1 & 2
(b)	eg 110 ÷ sin($\tan^{-1}(110/80)$)	award 1 of the first 2 marks

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
8	<p>Ans: 360 grams</p> <ul style="list-style-type: none"> •¹ strategy: know to calculate volume •² process: calculate volume •³ strategy: know to use proportion •⁴ strategy: carry out calculations correctly 	<ul style="list-style-type: none"> •¹ $10 \times 10 \times 3$ •² 300 •³ $\frac{300}{400} \times 480$ or equivalent •⁴ 360 <p style="text-align: right;">4 marks</p>
<p>1. Correct answer without working award 4/4</p> <p>2. Some common answers (no working necessary)</p> <p>(a) 380 [300 + 80] award 2/4 ✓✓××</p> <p>(b) 300 award 2/4 ✓✓××</p> <p>3. Some common answers (working must be shown)</p> <p>(a) $300 \div (480 \div 400) = 250$ award 3/4 ✓✓×✓</p> <p>(b) $300 \times (400 \div 480) = 250$ award 3/4 ✓✓×✓</p> <p style="padding-left: 40px;">[Do not penalise premature rounding eg $400 \div 480 = 0.8 \times 300 = 240$]</p> <p>4. Alternative strategy</p> <p>(a) $300 + 300 \div 5 = 360$ (no working necessary) award 4/4</p> <p>(b) $300 + 300 \div 6 = 350$ (working must be shown) award 3/4 ✓✓×✓</p>		

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
9	<p>Ans: £183.45</p> <ul style="list-style-type: none"> •¹ interpret/process: find cost of tickets in euros •² strategy: know how to convert cost into sterling •³ process: convert cost into sterling to the nearest penny 	<ul style="list-style-type: none"> •¹ 255 •² $255 \div 1.39$ •³ 183.45 <p style="text-align: right;">3 marks</p>

NOTES:

1. (a) Correct answer without working award 3/3
 (b) 354.45 [255×1.39] (no working necessary) award 1/3 ✓××
2. Alternative strategy

<ul style="list-style-type: none"> •¹ interpret/strategy: know how to convert valid number of euros into sterling 	<ul style="list-style-type: none"> •¹ $90 \div 1.39$ or $75 \div 1.39$ or $180 \div 1.39$
<ul style="list-style-type: none"> •² process: convert valid cost into sterling to the nearest penny 	<ul style="list-style-type: none"> •² $90 \div 1.39 = 64.74$ or 64.75 or $75 \div 1.39 = 53.95$ or 53.96 or $180 \div 1.39 = 129.49$ or 129.50
<ul style="list-style-type: none"> •³ interpret/strategy: find total cost of tickets in sterling 	<ul style="list-style-type: none"> •³ 183.43 or 183.44 or 183.45 or 183.46

3. Where working shows that candidate has used alternative strategy award 3/3 for final answers of 183.43, 183.44 or 183.46

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
10	Ans: $y > 20$ • ¹ process: collect constants • ² process: solve inequality for y	• ¹ $\frac{1}{2}y > 10$ • ² $y > 20$ <p style="text-align: right;">2 marks</p>

NOTES:

1. For answers without valid working award 1/2

eg (i) $y > 20$ without working

(ii) $\frac{1}{2} \times 20 + 3 > 13 \rightarrow y > 20$

2. Answers acceptable for partial credit (valid working must be shown)

(i) $\frac{1}{2}y > 10 \rightarrow y > 20$

(ii) $\frac{1}{2}y > 10 \rightarrow y = 20$ or $\frac{1}{2}y = 10 \rightarrow y = 20$ } award 1/2

(iii) $\frac{1}{2}y > 16 \rightarrow y > 32$

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
11	<p>Ans: 360 cm²</p> <ul style="list-style-type: none"> •¹ strategy: use correct tangent ratio •² process: know how to solve equation •³ process: carry out trig. calculation •⁴ strategy/process: calculate area of rectangle 	<ul style="list-style-type: none"> •¹ $\tan 58^\circ = \frac{L}{15}$ •² $L = 15 \tan 58^\circ$ •³ 24 •⁴ $24 \times 15 = 360$ <p style="text-align: right;">4 marks</p>

NOTES:

1. Some answers without working

(a) 360	award 4/4	
(b) 24	award 3/4	✓✓✓×

2. 1,874(…) (radians used) award 4/4
 290(…) (grad used) award 4/4

3. Where an incorrect trig ratio is used, working should be followed through with the possibility of awarding 3/4.
 [Do not penalise premature rounding]

(a) $15 \cos 58^\circ \times 15 = 119(\dots)$	award 3/4	×✓✓✓
(b) $15 \sin 58^\circ \times 15 = 191$ or $190(\dots)$	award 3/4	×✓✓✓
(c) $\tan 58^\circ = \frac{15}{L} \rightarrow (15 \div \tan 58^\circ) \times 15 = 141$ or $140(\dots)$	award 3/4	×✓✓✓
(d) $\cos 58^\circ = \frac{15}{L} \rightarrow (15 \div \cos 58^\circ) \times 15 = 425$ or $424(\dots)$	award 3/4	×✓✓✓
(e) $\sin 58^\circ = \frac{15}{L} \rightarrow (15 \div \sin 58^\circ) \times 15 = 265(\dots)$	award 3/4	×✓✓✓
(f) $\tan 58^\circ = \frac{15}{L} \rightarrow (\tan 58^\circ \div 15) \times 15 = 1.6(\dots)$	award 2/4	××✓✓
(g) $\tan^{-1}(58/15) \times 15 = 1132(\dots)$	award 2/4	××✓✓

4. 4th mark is available for correctly multiplying previously calculated value by 15

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
12	Ans: 0·91 • ¹ interpret/process: correctly multiply $2\cdot6 \times 1\cdot4$ • ² • ³ interpret/process: correctly divide $(2\cdot6 \times 1\cdot4) \div (2\cdot6 + 1\cdot4)$	• ¹ $2\cdot6 \times 1\cdot4 = 3\cdot64$ • ² • ³ $(2\cdot6 \times 1\cdot4) \div (2\cdot6 + 1\cdot4) = 0\cdot91$ [award 1 for $2\cdot6 \times 1\cdot4 \div 2\cdot6 + 1\cdot4 = 2\cdot8$] <div style="text-align: right;">3 marks</div>

NOTES:

1. Correct answer without working award 3/3

2. Some common answers (no working necessary)

(a) $2\cdot6 \times 1\cdot4 \div 2\cdot6 + 1\cdot4 = 2\cdot8$	award 2/3	✓✓×
(b) $3\cdot64 \div 4 = 0\cdot9$	award 2/3	✓✓×
(c) $\frac{3\cdot64}{4}$	award 1/3	✓××
(d) $\frac{2\cdot6 \times 1\cdot4}{2\cdot6 + 1\cdot4}$ or $\frac{2\cdot6 \times 1\cdot4}{4}$	award 0/3	

3. Some common answers (working must be shown)

(a) $\frac{4}{2\cdot6 + 1\cdot4} = 4 \div 2\cdot6 + 1\cdot4 = 2\cdot9(\dots)$	award 1/3	×✓×
(b) $\frac{4}{4} = 1$ (calculation eased)	award 1/3	×✓×

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
14	<p>Ans: 63 m²</p> <ul style="list-style-type: none"> •¹ strategy: know to calculate area of semi-circle •² strategy: substitute correct radius into area formula •³ strategy: know to add area of triangle to area of semi-circle •⁴ process: carry out all calculations correctly (must include a circle calculation involving either squaring or halving followed by an addition or a subtraction) 	<ul style="list-style-type: none"> •¹ $\frac{1}{2} \pi r^2$ •² $\frac{1}{2} \times \pi \times 5^2$ •³ $\frac{1}{2} \times \pi \times 5^2 + \frac{1}{2} \times 8 \times 6$ •⁴ $63(\cdot 2699\dots)$ or $63(\cdot 25)$ (π) (3·14) <p style="text-align: right;">4 marks</p>

NOTES:

1. Correct answer without working award 0/4
2. **Beware!!!**
 3rd mark not available for adding $8+6+10=24$ to area of semi-circle
 eg (i) $\frac{1}{2} \times \pi \times 5^2 + \frac{1}{2} \times 8 \times 6 = 63$ award 4/4
 (ii) $\frac{1}{2} \times \pi \times 5^2 + 8+6+10 = 63$ award 3/4 ✓✓×✓
 (iii) $\frac{1}{2} \times \pi \times 5^2 + 24 = 63$ award 3/4 ✓✓×✓
3. Some common answers (working must be shown)

(a) 181(·...)	$[\frac{1}{2}\pi r^2 + \frac{1}{2} \times 8 \times 6, r=10]$	award 3/4	✓×✓✓
(b) 157(·...)	$[\frac{1}{2}\pi r^2, r=10]$	award 1/4	✓×××
(c) 102(·...), 103	$[\pi r^2 + \frac{1}{2} \times 8 \times 6]$	award 3/4	×✓✓✓
(d) 87(·...)	$[\frac{1}{2}\pi r^2 + 48]$	award 3/4	✓✓×✓
(e) 79,78(·...)	$[\pi r^2]$	award 1/4	×✓××
(f) 79(·...)	$[\pi d + 48, d=10]$	award 1/4	×✓××
(g) 63(·...), 64	$[\frac{1}{2}\pi r^2 + 48, r^2=5^2=10]$	award 2/4	✓✓××
(h) 63(·...), 64	$[\frac{1}{2}\pi d + 48, d=10]$	award 2/4	×✓×✓
(i) 55(·...)	$[\pi r^2 + \frac{1}{2} \times 8 \times 6, r^2=5^2=10]$	award 2/4	×✓✓×
(j) 55(·...)	$[\pi d + \frac{1}{2} \times 8 \times 6, d=10]$	award 2/4	×✓✓×
(k) 39(·...), 40	$[\frac{1}{2}\pi r^2 + \frac{1}{2} \times 8 \times 6, r^2=5^2=10]$	award 3/4	✓✓✓×
(l) 39(·...), 40	$[\frac{1}{2}\pi d + \frac{1}{2} \times 8 \times 6, d=10]$	award 3/4	×✓✓✓
(m) 39(·...)	$[\frac{1}{2}\pi r^2]$	award 2/4	✓✓××

TOTAL MARKS FOR PAPER 2

50

**TOTAL MARKS FOR
PAPER 1 & 2**

80

[END OF MARKING INSTRUCTIONS]